



BSI Standards Publication

## Information technology database languages — SQL technical reports

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Part 8: Multi-dimensional arrays (SQL/MDA)

## National foreword

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**Part 8:  
Multi-dimensional arrays (SQL/MDA)**

*Langages de base de données IT — SQL rapport techniques —  
Partie 8: Tableaux multidimensionnels*



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<b>Contents</b>	Page
Foreword.....	vii
Introduction.....	viii
<b>1 Scope.....</b>	<b>1</b>
<b>2 Normative references.....</b>	<b>3</b>
<b>3 Terms and definitions.....</b>	<b>5</b>
<b>4 Multidimensional Arrays (MDA) concepts.....</b>	<b>7</b>
4.1 Concept.....	7
4.2 Why consider support for MDA in SQL?.....	7
4.3 Array representations.....	9
4.4 Use cases for MDA support in SQL.....	9
4.4.1 The use cases.....	9
4.4.2 Array data ingestion and storage.....	9
4.4.3 Integrated querying of array and relational data.....	10
4.4.4 Updating stored array data.....	10
4.4.5 Exporting arrays.....	10
4.5 Non-Use cases: Direct access to external array data.....	10
<b>5 SQL/MDA data model.....</b>	<b>11</b>
5.1 Data model concepts.....	11
5.2 MD-array.....	11
5.3 MD-array type definition.....	12
5.3.1 Type definition concepts.....	12
5.3.2 Element type.....	12
5.3.3 MD-dimension.....	13
5.3.4 MD-axis names.....	13
5.3.5 MD-axis lower and upper limits.....	13
5.3.6 Putting it all together.....	14
5.4 MD-array creation.....	16
5.4.1 MD-array creation concepts.....	16
5.4.2 Explicit element enumeration.....	17
5.4.3 From SQL table query result.....	18
5.4.4 Construction by implicit iteration.....	19
5.4.5 Decoding a format-encoded array.....	20
5.5 MD-array updating.....	21
5.5.1 MD-array updating introduction.....	21
5.5.2 Updating MD-arrays of equal MD-dimension.....	22
5.5.3 Updating MD-arrays of greater MD-dimension.....	23
5.5.4 Updating a single element of an MD-array.....	24
5.6 Exporting MD-arrays.....	24

**ISO/IEC TR 19075-8:2019(E)**

5.6.1	Encoding to a data format. . . . .	24
5.6.2	Converting to an SQL table. . . . .	26
<b>6</b>	<b>SQL/MDA operations. . . . .</b>	<b>29</b>
6.1	Introduction to SQL/MDA operations. . . . .	29
6.2	MD-extent probing operators. . . . .	29
6.3	MD-array element reference. . . . .	31
6.4	MD-extent modifying operations. . . . .	32
6.4.1	Introduction to MDE-extent modifying operations. . . . .	32
6.4.2	Subsetting. . . . .	32
6.4.3	Reshaping. . . . .	34
6.4.4	Shifting. . . . .	36
6.4.5	MD-axis renaming. . . . .	36
6.5	MD-array deriving operators. . . . .	37
6.5.1	Introduction to MD-array deriving operators. . . . .	37
6.5.2	Scaling. . . . .	37
6.5.3	Concatenation. . . . .	39
6.5.4	Induced operations. . . . .	39
6.5.5	Join MD-arrays on their coordinates. . . . .	46
6.6	MD-array aggregation. . . . .	47
6.6.1	General aggregation expression. . . . .	47
6.6.2	Shorthand aggregation functions. . . . .	48
<b>7</b>	<b>Remote sensing example. . . . .</b>	<b>51</b>
7.1	Introduction to remote sensing example. . . . .	51
7.2	Data setup. . . . .	51
7.3	Band math. . . . .	53
7.3.1	Introduction to band math. . . . .	53
7.3.2	NDVI. . . . .	53
7.3.3	Band Swapping. . . . .	56
7.4	Histograms. . . . .	57
7.5	Change detection. . . . .	58
7.6	Extracting features. . . . .	59
7.7	Data search and filtering. . . . .	60
	<b>Bibliography. . . . .</b>	<b>63</b>
	<b>Index. . . . .</b>	<b>65</b>

## Tables

<b>Table</b>		<b>Page</b>
1	Examples of MD-array type definitions. . . . .	15
2	Examples of MD-arrays constructed by element enumeration. . . . .	18
3	Examples of MD-arrays created with the constructor by iteration. . . . .	20
4	Examples of MD-arrays created from JSON-encoded arrays. . . . .	21
5	Examples of MD-arrays encoded to JSON arrays. . . . .	25
6	Result of example UNNEST query. . . . .	26
7	Result of example UNNEST query specifying WITH ORDINALITY. . . . .	27
8	Examples with MD-extent probing functions. . . . .	30
9	Result of MDEXTENT(kernel). . . . .	30
10	Result of MDEXTENT_MAX(kernel). . . . .	30
11	Examples of referencing a single element in an MD-array. . . . .	31
12	Examples of MD-array subsetting. . . . .	34
13	Examples of MD-extent reshaping. . . . .	35
14	Examples of MD-extent shifting. . . . .	36
15	Examples of MD-axis renaming. . . . .	37
16	Interpolation methods defined in <a href="#">ISO 19123:2005</a> . . . . .	38
17	Examples of MD-array concatenation. . . . .	39
18	Examples of induced function application to MD-arrays. . . . .	42
19	Operations corresponding to the <md-array value expression> grammar rules. . . . .	44
20	Examples of induced MD-array expressions. . . . .	44
21	Example of induced MD-array casting. . . . .	45
22	Examples of induced CASE expression. . . . .	45
23	Examples of MDJOIN. . . . .	47
24	Identity elements for the <md-array aggregation operator>s. . . . .	47
25	Examples of general MD-array aggregation. . . . .	48
26	Predefined aggregation operators. . . . .	49
27	Landsat TM bands. . . . .	51

## Figures

<b>Figure</b>	<b>Page</b>
1 Aerial greyscale image of size 1024x1024 (San Diego). . . . .	8
2 Relationships between MDA and SQL/MDA. . . . .	11
3 The structure of an MD-array value illustrated on a sample 3x3 array. . . . .	12
4 Placement of satellite images of each country on a world map (from <a href="#">Geographic Bounding Boxes</a> ). . . . .	14
5 Example of an SQL table that corresponds to a 3x3 MD-array. . . . .	19
6 Example of an SQL table converted to a 3x3 MD-array with MD-extent [i(-1:1), j(-1:1)]. . . . .	19
7 Example of array update. . . . .	23
8 Updating a 3-D MD-array with a 2-D source MD-array. . . . .	24
9 MD-array subsetting examples. . . . .	32
10 MD-array reshaping example. . . . .	35
11 MD-array shifting example. . . . .	36
12 MD-array scaling example. . . . .	37
13 Concatenation examples. . . . .	39
14 Example of summing two MD-arrays. . . . .	40
15 Colorized array. . . . .	46
16 Visible color (RGB) bands of a Landsat TM scene. . . . .	52
17 NDVI result stretched to the range (0,255). . . . .	54
18 NDVI values between 0.2 and 0.4 shown in white, while everything else is black. . . . .	55
19 Color-mapped NDVI result, from dark blue, through grey, to dark green. . . . .	56
20 False color image constructed from the near IR, red and green bands. . . . .	57
21 Histogram of the NDVI index of a Landsat TM scene. . . . .	58
22 A composite image with an NDVI index from different years in each channel. . . . .	59
23 Natural RGB color of barrier islands area. . . . .	60
24 Binary image showing isolated islands. . . . .	60

## Foreword

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## **Introduction**

This Technical Report describes the definition and use of multi-dimensional arrays in SQL. Multidimensional arrays represent a core underlying structure of manifold science and engineering data. It is generally recognized today, therefore, that arrays have an essential role in Big Data and should become an integral part of the overall data type orchestration in information systems. This Technical Report discusses the syntax and semantics of operations on the MD-array data type defined in [ISO/IEC 9075-15](#).

The organization of this Technical Report is as follows:

- 1) [Clause 1, “Scope”](#), specifies the scope of this Technical Report.
- 2) [Clause 2, “Normative references”](#), identifies standards that are referenced by this Technical Report.
- 3) [Clause 4, “Multidimensional Arrays \(MDA\) concepts”](#), introduces the concept of Multidimensional Arrays.
- 4) [Clause 5, “SQL/MDA data model”](#), introduces the data model.
- 5) [Clause 6, “SQL/MDA operations”](#), covers the supported operations on MD-arrays..
- 6) [Clause 7, “Remote sensing example”](#), illustrates the supported functionality through realistic examples.

## **Information technology database languages — SQL technical reports —**

Part 8:

### **Multi-dimensional arrays (SQL/MDA)**

#### **1 Scope**

This Technical Report describes the support in SQL for Multi-Dimensional Arrays (MDA) as defined in [ISO/IEC 9075-15](#).